I retired from my faculty position at the end of 2003, but remained active in research.

Per *Ecclesiastes*, "of making many books there is no end." The notes from Math 301–305 (Analysis) were turned into a textbook – my second undergraduate analysis textbook. (The first, published in 1973, tried to use the theory of distributions to make everything easier. It has seen little use, even by me.) The newer text, *Analysis, an Introduction*, was published by Cambridge in 2004. It is much more classical in approach, and gets to some fun topics including Euler's product formula for  $\sin x$ , the Banach–Tarski paradox, and the Heisenberg uncertainty principle. It has been used for Math 301-305 at Yale but, judging from the yearly sales, sees little use elsewhere. For anyone who might be interested, the table of contents and a list of corrections are appended.

Through various research projects I was drawn, reluctantly, into a passing acquaintance with special functions (the ones that you don't learn about in calculus but that have names nonetheless). Some random events led to co-authoring a book on the subject, with Roderick Wong of the City University of Hong Kong, who is an actual expert in the subject. Cambridge University Press took it on as well: *Special Functions, a Graduate Text.* See below end for a few corrections. A second, enlarged, edition, is retitled as *Special Functions and Orthogonal Polynomials*; its table of contents is given below.

Several post-retirement stints teaching the advanced complex analysis course showed me that the wonderful thing about the course is that there are too many great topics to cover in one iteration, so that the instructor and the class get to make some choices. So of course one needs a book to cover a large selection of topics – and Wong and I have produced one, *Explorations in Complex Functions*, published by Springer in 2020. Again, the table of contents is given below.

Explorations did not exhaust the possible topics, but it was going to be our final book ... until both Roderick and I decided that we needed another project. Hence More Explorations in Complex Functions, published by Springer in 2023; table of contents below.

# Tables of Contents, in reverse chronological order

## More Explorations in Complex Functions – Contents:

- 1. Basics
- 2. Further preliminaries
- 3. Complex Dynamics
- 4. Univalent functions and de Branges's theorem
- 5. Harmonic and subharmonic functions; the Dirichlet problem
- 6. General Riemann surfaces
- 7. The uniformization theorem
- 8. Quasiconformal mapping
- 9. Introduction to Teichmüller theory
- 10. The Bergman kernel
- 11. Theta functions
- 12. Padé approximations and continued fractions
- 13. Riemann–Hilbert problems
- 14. Asymptotics and Darboux's method

### **Explorations in Complex Functions** – Contents:

- 1. Basics
- 2. Linear fractional transformations
- 3. Hyperbolic geometry
- 4. Harmonic functions
- 5. Conformal maps and the Riemann mapping theorem
- 6. The Schwarzian derivative
- 7. Riemann surfaces and algebraic curve
- 8. Entire functions
- 9. Value distribution theory
- 10. The gamma and beta functions
- 11. The Riemann zeta function
- 12. L-functions and primes
- 13. The Riemann hypothesis
- 14. Elliptic functions and theta functions
- 15. Jacobi elliptic functions
- 16. Weierstrass elliptic functions
- 17. Automorphic functions and Picard's theorem
- 18. Integral transforms
- 19. Theorems of Phragmén–Lindelöf and Paley–Wiener
- 20. Theorems of Wiener and Lévy; the Wiener-Hopf method
- 21. Tauberian theorems
- 22. Asymptotics and the method of steepest descent
- 23. Complex interpolation and the Riesz-Thorin theorem

### Special Functions and Orthogonal Polynomials – Contents:

- 1. Introduction
- 2. Gamma, beta, zeta
- 3. Second–order differential equations
- 4. Orthogonal polynomials on an interval
- 5. The classical orthogonal polynomials
- 6. Semi-classical orthogonal polynomials
- 7. Asymptotics of orthogonal polynomials: two methods
- 8. Confluent hypergeometric functions
- 9. Cylinder functions
- 10. Hypergeometric functions
- 11. Spherical functions
- 12. Generalized hypergeometric functions; G-functions
- 13. Asymptotics
- 14. Elliptic functions
- 15. Painlevé transcendents
- Appendix A. Complex analysis

Appendix B. Fourier analysis

#### Analysis, an Introduction – Contents:

- 1. Introduction
- 2. The Real and Complex Numbers
- 3. Real and Complex Sequences
- 4. Series
- 5. Power Series
- 6. Metric Spaces
- 7. Continuous Functions
- 8. Calculus
- 9. Some Special Functions
- 10. Lebesgue Measure on the Line
- 11. Lebesgue Integration on the Line
- 12. Function Spaces
- 13. Fourier Series
- 14. Applications of Fourier Series
- 15. Ordinary Differential Equations

### Corrections to Analysis. An Introduction

I am indebted to Mary Pugh, Gerard Misiolek, and José Rodrigo for most of the following corrections. And I am especially indebted to Eric Belsley, whose detailed comments on the notes for chapters 1-9 are the chief reason there are so few corrections for those chapters. (The exercises on page 130 were added later!)

- p. 6, eqn. (14): (m-n)+(p-q)=(m+p)-(n+q)
- p. 7, line 9: ... and satisfies M1, M2,

p. 26, exercise 2: (ii)  $1, x, x^2, \dots x^n$  are linearly dependent over  $\mathbb{Q}$ .

exercise 2: (iv) there are real numbers  $y_1, y_2, \ldots y_n$  such that  $\ldots$ 

- p. 28, line 16:  $= |z|^2 + 2\text{Re}(z\bar{w}) + |w|^2 \leq \dots$
- p. 66, exercise 4: right side should be  $1/(1-z)^{k+1}$ .

exercise 5: Under the given assumptions, show there is a power series  $\sum_{n=0}^{\infty} b_n z^n$  with radius of convergence at least R - r such that

$$\sum_{n=0}^{\infty} a_n z^n = \sum_{n=0}^{\infty} b_n (z - z_0)^n, \qquad |z - z_0| < R - r.$$

- p. 103, line 3: = f'(c)[g(b) g(a)] g'(c)[f(b) f(a)];line 4: divide by [g(b) - g(a)]g'(c).
- p. 115, lines 1-2: Suppose that f is a real-valued function ...
- p. 124, equation (14):  $z^n + a_{n-1}z^{n-1} + \dots$
- p. 130, exercise 8: F(a, b, c; z)exercise 9: F(a, b, b; z)exercise 10:  $\int_0^1 t^{b-1} (1-t)^{c-b-1} (1-tz)^{-a} dt$

p. 137, line 6: ...  $+ m^*((E \cap (A \cup B)) \cap A^c)$ p. 149, line 8: ... for  $x \in [0, 1] \cap C^c$  ... p. 152, line 13:  $\int \int (f+g)$  should be  $\int (f+g)$ p. 170, line 9:  $\{h^* > \delta/2\}, \{h > \delta/2\}$ p. 171, line 5: ... and define a subfamily  $\mathcal{I}_{n+1}$  ... line 6: ... if  $\mathcal{I}_{n+1}$  is empty ... line 11: ... implies that  $|I_k| \ge |I|/2 \dots$ line -10: ...  $I \subset I_n^*$  for some n. p. 178, equation (17): omit  $1/2\pi$ p. 181, line -9:  $\sum_{n=0}^{2N} (e^{ix})^n$ line -11: ... as long as  $e^{ix} \neq 1$ ,  $S_N f(x_0) - f(x_0) = \dots$ p. 183, line 9: line 10: ...  $[f(x_0 - y) - f(x_0)] dy$ equation (31):  $\sin\left(\left[N+\frac{1}{2}\right]y\right)$ p. 186, line -5,-4: ... property (ii) in Proposition 13.9 ... line -2:  $\int_{|y|<\delta}$ line -1:  $\int_{\delta < |u| < \pi}$ p. 189, line -4: See Exercise 9 of Section 12D.  $f_N(x) = \sum_{-N}^N a_n e^{inx}$ p. 192, line 8: p. 192, line -2:  $a_0 = 0$ p. 193, line 3: Use Exercise 5 of this section and ... p. 194, exercise 10:  $f(x_0-) = \lim_{x \to x_0, x < x_0} f(x); \dots$ p. 196, exercise 4:  $g_n(x) = ...$ p. 201, equation (6):  $0 \le t \le 2\pi$ p. 211, line 5: ... let  $I_L = [-\frac{1}{2}L, \frac{1}{2}L] \dots$ line 8:  $\int_{-L/2}^{L/2}$ p. 214, exercise 6:  $f(x) = \frac{1}{\sqrt{2\pi}}e^{-x^2/2}$ p. 215, exercise 9: ... (assume (46) and use Dominated Convergence). p. 217, equation (57):  $V_T = ||(T - E_T I)\psi||^2$ p. 227, line 11: ... but it may not be unique. p. 234, line 1: f(x, y)

p. 238, proof of Lemma 238. It might seem at first that the sets removed from  $A_2$  and  $A_3$  to form  $A_2$  and  $A_4$  are empty, but there is a nonzero vector that is fixed by  $\sigma$ .

p. 239, statement of Theorem: there should be four  $B'_j$  and three  $C'_j$ : drop  $C'_4$  and take

$$B'_{j} = B_{j} \cap (D_{f} \cup D_{\infty}), \quad j = 1, 2; \qquad B'_{j} = B_{j-2} \cup D_{g}, \quad j = 3, 4$$

Then the first four  $A'_i$  correspond to the  $B'_i$  and the last three to the  $C'_i$ .

Also:  $f: D_{\infty} \to A_{\infty}$  and  $g: A_{\infty} \to D_{\infty}$  are bijective (but not inverses of each other).

p. 243, Section 3A: Omit 12, and renumber 13 - 17 as 12 - 16.

p. 251, Section 13B, 6 (b): ... the interval  $[b, b + 2\pi)$  ...

p. 252, Section 13G: 1, 2. Use Theorems 13.12 and 13.14 and Proposition 13.4. Note that a continuous periodic function is an  $L^2$ -periodic function. For exercise 1 (b), continuity or lack of continuity can be seen by comparison with a multiple of the square wave function in §14A.