Homework 14

1. Find the general solution to the following ODEs

(a)
$$y'' + 2y' + y = 5$$

(b)
$$y'' - 5y' + 6y = t + 6$$

(c)
$$y'' - 5y' + 6y = te^t$$

(d)
$$y'' + y = e^t$$

(e)
$$y'' + y = 3\sin 2t + 6\cos 2t$$

2. Find the general solution to the following ODEs.

(a)
$$y'' - 5y' + 6y = e^{3t}$$

(b)
$$y'' + y = \sin t$$

(c)
$$y'' + 2y' + y = te^{-t}$$

(d)
$$y'' + 2y' - 3y = e^{-3t} + \sin 2t$$

3. Let ω_0 be a constant real number and let ω be another constant real number with $\omega \neq \omega_0$. Solve the following IVPs

(a)
$$y'' + \omega_0^2 y = \cos \omega t$$
, $y(0) = 0$, $y'(0) = 0$

(b)
$$y'' + \omega_0^2 y = \cos \omega_0 t$$
, $y(0) = 0$, $y'(0) = 0$