408L CLASS PROBLEMS

MARCH 9TH, 2020

Problem 1. For each of the following functions f(x, y), find $\frac{\partial}{\partial x} f(x, y)$ and $\frac{\partial}{\partial y} f(x, y)$.

(1) $f(x, y) = x^2 + 2xy + y^2$. (2) $f(x, y) = \sin(xy)$. (3) $f(x, y) = ye^{x^2 + y^2}$. (4) $f(x, y) = \frac{x}{y}$. (5) $f(x, y) = x^y$.

Problem 2. The Laplace equation $(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2})f(x,y) = 0$ tells when a function f(x,y) returns the temperature of a 2-dimensional room at thermal equilibrium.

Which of the following functions satisfy the heat equation?

(1)
$$f(x, y) = xy$$
.
(2) $f(x, y) = x^2 - y^2$.
(3) $f(x, y) = x^2 + y^2$.
(4) $f(x, y) = \log(x^2 + y^2)$
(5) $f(x, y) = \frac{x}{x^2 + y^2}$.
(6) $f(x, y) = \sin(y)e^x$.